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Getting help

Are you getting enough help and support?

A. Yes

- B. No because I didn't realize there were office hours
- C. No because the office hours are at a time that I can't make
- D. No because I'm embarrassed to ask for help
- E. No because of some other reason

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Project

How is the project going?

- A. Easy, getting it all done quickly and easily
- B. Challenging but doable
- C. Very challenging, I'm having a hard time
- D. Have no clue where to start

Recall worklist algorithm

let m: map from edge to computed value at edge
let worklist: work list of nodes

```
for each edge e in CFG do
m(e) := Ø
```

for each node n do worklist.add(n)

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Using lattices

- · We formalize our domain with a powerset lattice
- · But more generally ANY lattice
- · What should be top and what should be bottom?

Using lattices

- · We formalize our domain with a powerset lattice
- · But more generally ANY lattice
- · What should be top and what should be bottom?
- · Does it matter? It matters because, as we've seen, there is a notion of approximation, and this notion shows up in the lattice

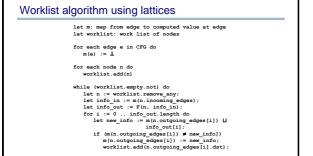
Using lattices

- Unfortunately:
 - dataflow analysis community has picked one direction
 - abstract interpretation community has picked the other
- · We will work with the abstract interpretation direction
- Bottom is the most precise (optimistic) answer, Top the most imprecise (conservative)

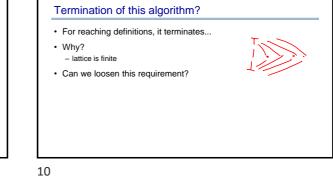
Direction of lattice

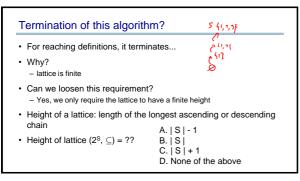
- · Always safe to go up in the lattice
- + Can always set the result to \top
- · Hard to go down in the lattice
- · Bottom will be the empty set in reaching defs

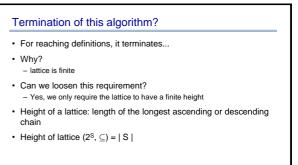
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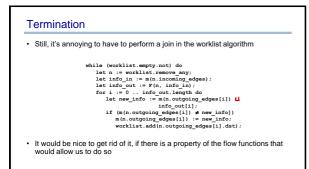


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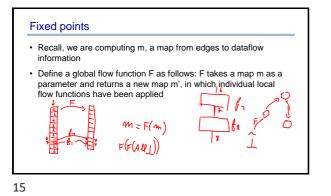




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Even more formal • To reason more formally about termination and precision, we reexpress our worklist algorithm mathematically • We will use fixed points to formalize our algorithm

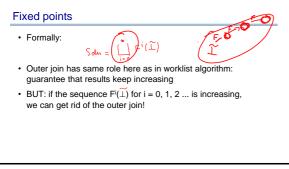
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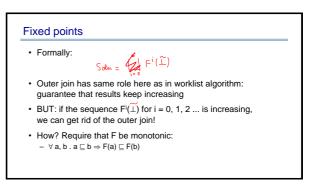


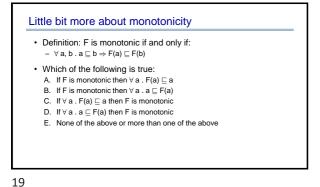
Fixed points

- We want to find a fixed point of F, that is to say a map m such that m=F(m)
- · Approach to doing this?
- Define $\widetilde{\perp}$, which is \perp lifted to be a map: $\widetilde{\perp} = \lambda \text{ e. } \perp$
- Compute F(⊥), then F(F(⊥)), then F(F(F(⊥))), ... until the result doesn't change anymore



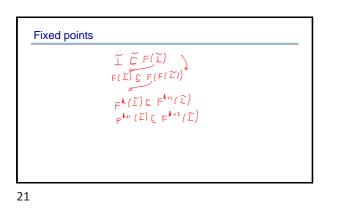






Fixed points $F(\widehat{L}) \subseteq FF(L)$ $\widehat{\downarrow} \subseteq F(\widehat{L})$

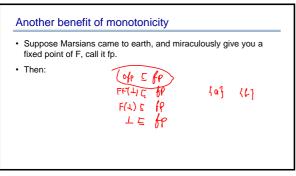
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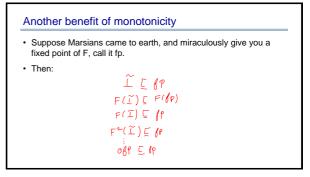


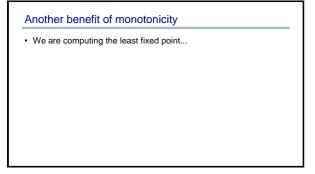


- So if F is monotonic, we have what we want: finite height \Rightarrow termination, without the outer join
- Also, if the local flow functions are monotonic, then global flow function ${\sf F}$ is monotonic







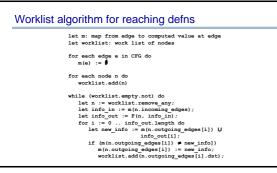


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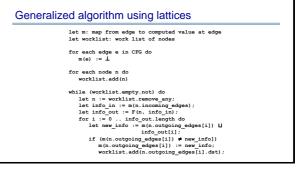
Recap

- · Let's do a recap of what we've seen so far
- · Started with worklist algorithm for reaching definitions

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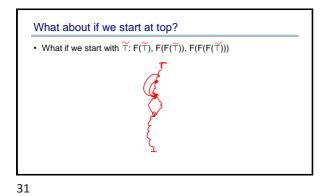
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Next step: removed outer join

- Wanted to remove the outer join, while still providing termination guarantee
- · To do this, we re-expressed our algorithm more formally
- We first defined a "global" flow function F, and then expressed our algorithm as a fixed point computation

Guarantees

- · If F is monotonic, don't need outer join
- If F is monotonic and height of lattice is finite: iterative algorithm terminates
- If F is monotonic, the fixed point we find is the least fixed point.



What about if we start at top?

- What if we start with $\stackrel{\sim}{\top}:$ F($\stackrel{\sim}{\top}),$ F(F($\stackrel{\sim}{\top})),$ F(F(F($\stackrel{\sim}{\top})))$
- · We get the greatest fixed point
- Why do we prefer the least fixed point?
 More precise

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