**Dataflow analysis** 

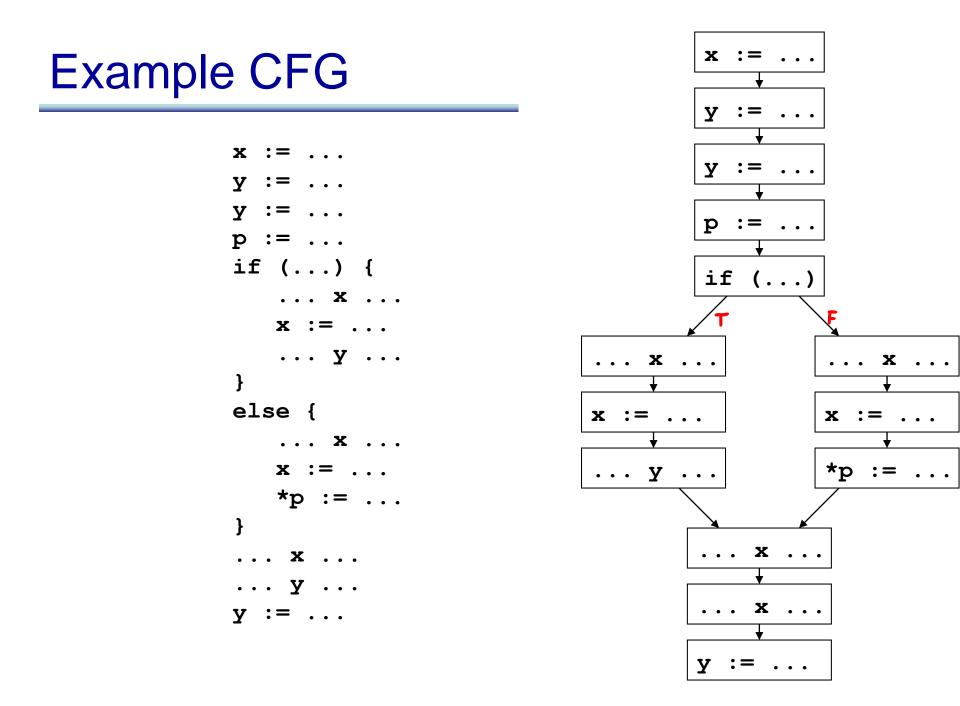
#### Dataflow analysis: what is it?

- A common framework for expressing algorithms that compute information about a program
- Why is such a framework useful?
- Provides a common language, which makes it easier to:
  - communicate your analysis to others
  - compare analyses
  - adapt techniques from one analysis to another
  - reuse implementations (eg: dataflow analysis frameworks)

# **Control Flow Graphs**

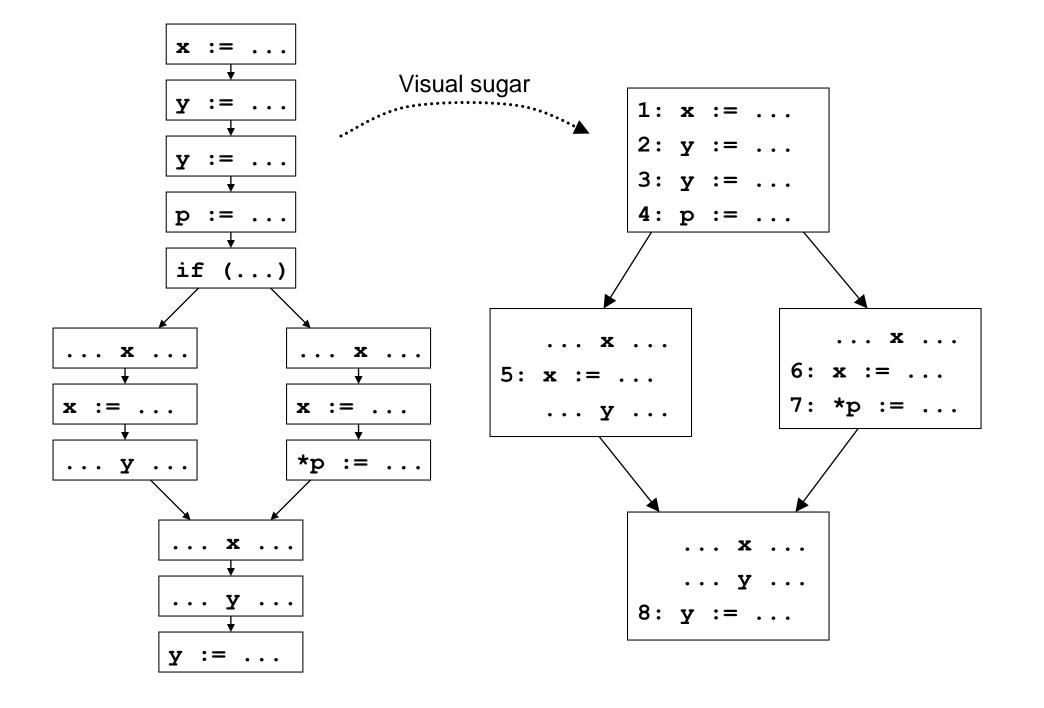
- For now, we will use a Control Flow Graph representation of programs
  - each statement becomes a node
  - edges between nodes represent control flow

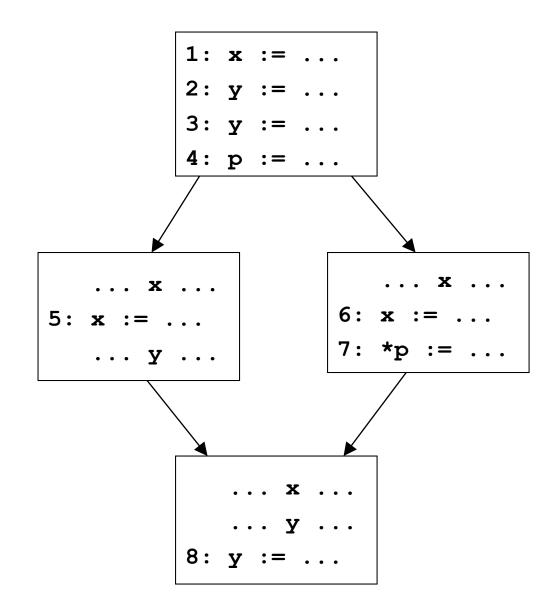
- Later we will see other program representations
  - variations on the CFG (eg CFG with basic blocks)
  - other graph based representations

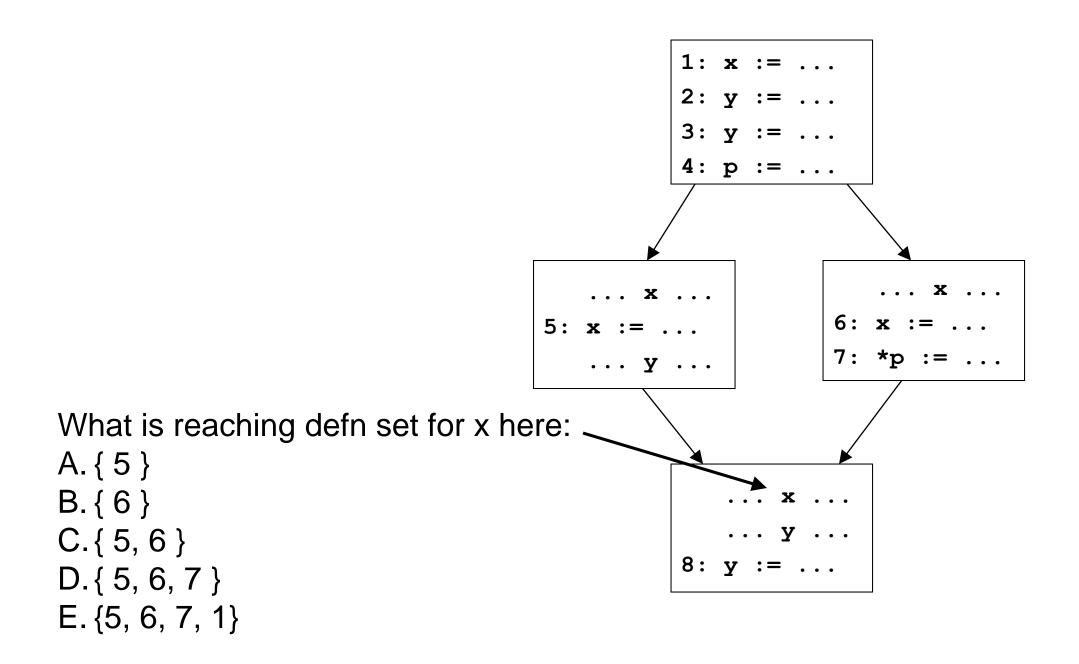


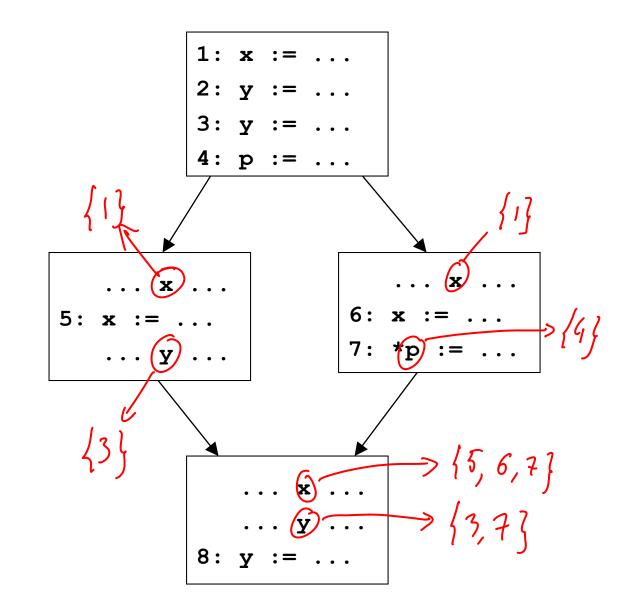
## An example DFA: reaching definitions

- For each use of a variable, determine what assignments could have set the value being read from the variable
- Information useful for:
  - performing constant and copy prop
  - detecting references to undefined variables
  - presenting "def/use chains" to the programmer
  - building other representations, like the DFG
- Let's try this out on an example









# Safety

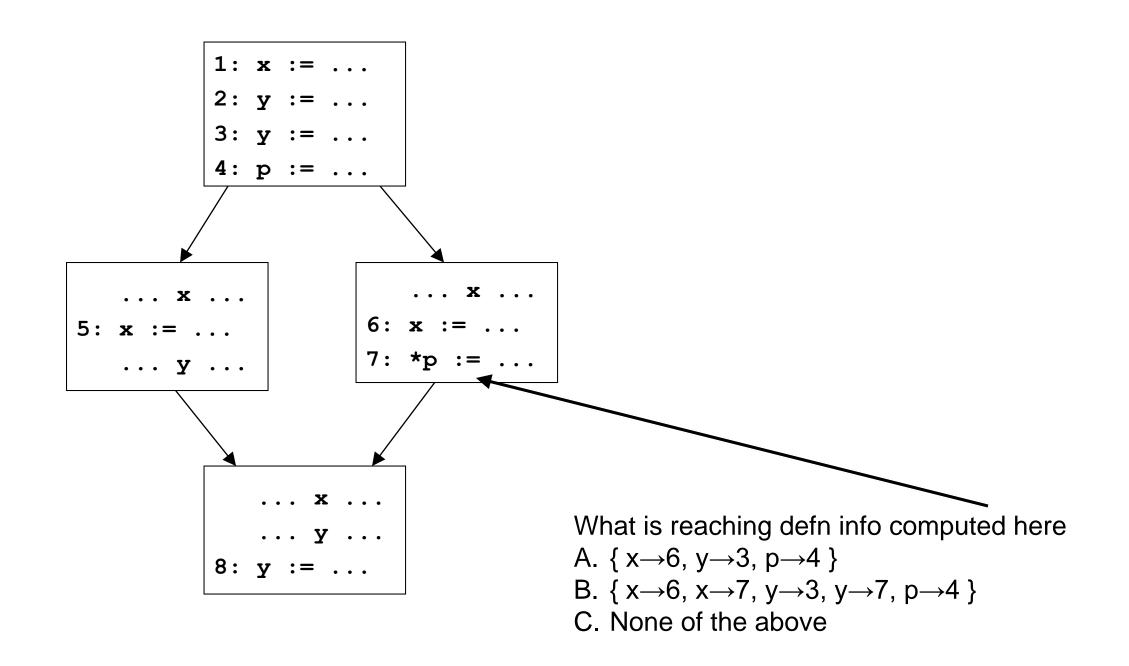
- When is computed info safe?
- Recall intended use of this info:
  - performing constant and copy prop
  - detecting references to undefined variables
  - presenting "def/use chains" to the programmer
  - building other representations, like the DFG
- Safety:
  - can have more bindings than the "true" answer, but can't miss any

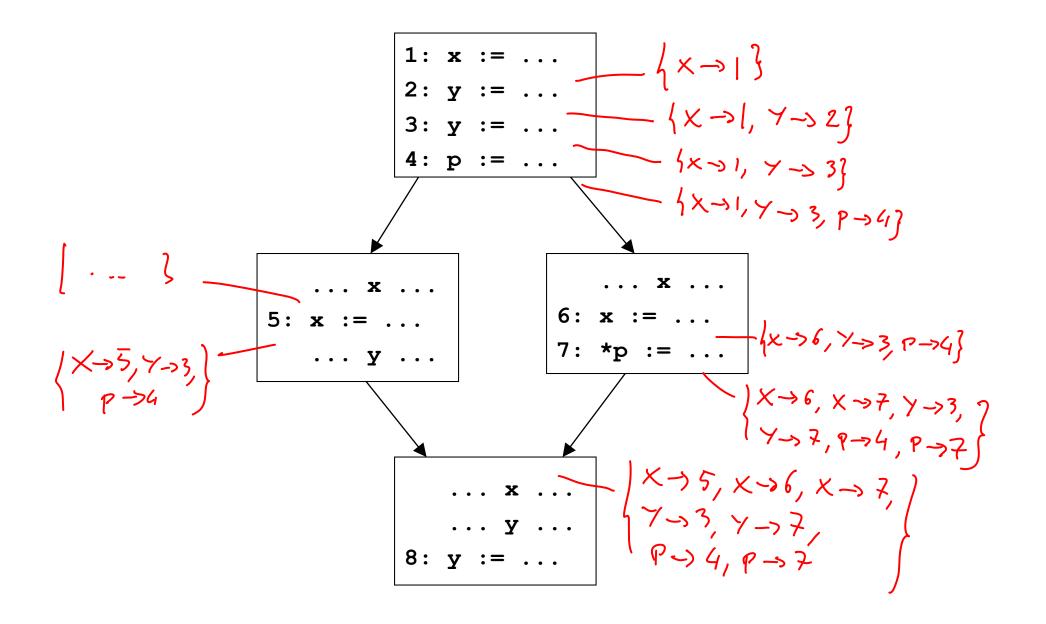
## Reaching definitions generalized

- DFA framework geared to computing information at each program point (edge) in the CFG
  - So generalize problem by stating what should be computed at each program point
- For each program point in the CFG, compute the set of definitions (statements) that may reach that point
- Notion of safety remains the same

# Reaching definitions generalized

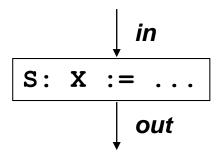
- Computed information at a program point is a set of var  $\rightarrow$  stmt bindings
  - eg: {  $x \rightarrow s_1, x \rightarrow s_2, y \rightarrow s_3$  }
- How do we get the previous info we wanted?
  - if a var x is used in a stmt whose incoming info is in,
  - then:  $\{ s \mid (x \rightarrow s) \in in \}$
- This is a common pattern
  - generalize the problem to define what information should be computed at each program point
  - use the computed information at the program points to get the original info we wanted

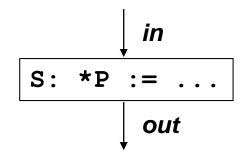


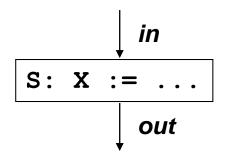


## Using constraints to formalize DFA

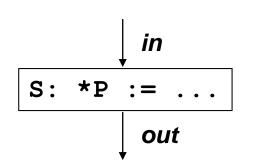
- Now that we've gone through some examples, let's try to precisely express the algorithms for computing dataflow information
- We'll model DFA as solving a system of constraints
- Each node in the CFG will impose constraints relating information at predecessor and successor points
- Solution to constraints is result of analysis







out = in – { 
$$X \rightarrow S' \mid S' \in stmts$$
 }  $\cup$  {  $X \rightarrow S$  }

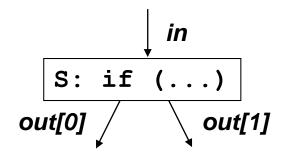


• Using may-point-to information:

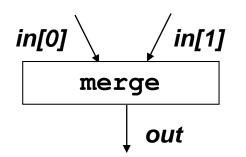
out = in  $\cup$  { X  $\rightarrow$  S | X  $\in$  may-point-to(P) }

• Using must-point-to aswell:

 $\begin{array}{ll} \text{out} = \text{in} - \left\{ \begin{array}{ll} X \rightarrow S' \mid X \in \text{must-point-to}(P) \\ S' \in \text{stmts} \end{array} \right\} \\ \cup \left\{ \begin{array}{ll} X \rightarrow S \mid X \in \text{may-point-to}(P) \end{array} \right\} \end{array}$ 



 $out [0] = in \land$  out [1] = inmore generally:  $\forall i . out [i] = in$ 



$$out = in [0] \cup in [1]$$
  
more generally:  $out = \bigcup_i in [i]$ 

# Flow functions

- The constraint for a statement kind s often have the form: out =  $F_s(in)$
- $F_s$  is called a flow function
  - other names for it: dataflow function, transfer function
- Given information in before statement s, F<sub>s</sub>(in) returns information after statement s
- Other formulations have the statement s as an explicit parameter to F: given a statement s and some information in, F(s,in) returns the outgoing information after statement s

## Flow functions, some issues

Issue: what does one do when there are multiple input edges to a node?

 Issue: what does one do when there are multiple outgoing edges to a node?

## Flow functions, some issues

- Issue: what does one do when there are multiple input edges to a node?
  - the flow functions takes as input a tuple of values, one value for each incoming edge
- Issue: what does one do when there are multiple outgoing edges to a node?
  - the flow function returns a tuple of values, one value for each outgoing edge
  - can also have one flow function per outgoing edge

## Flow functions

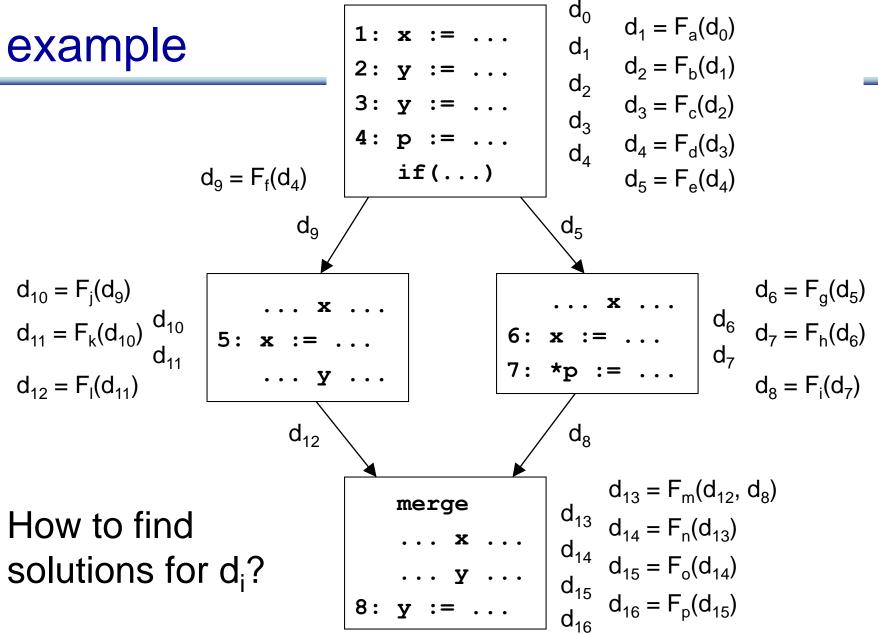
- Flow functions are a central component of a dataflow analysis
- They state constraints on the information flowing into and out of a statement

- This version of the flow functions is local
  - it applies to a particular statement kind
  - we'll see global flow functions shortly...

# Summary of flow functions

- Flow functions: Given information in before statement s, F<sub>s</sub>(in) returns information after statement s
- Flow functions are a central component of a dataflow analysis
- They state constraints on the information flowing into and out of a statement

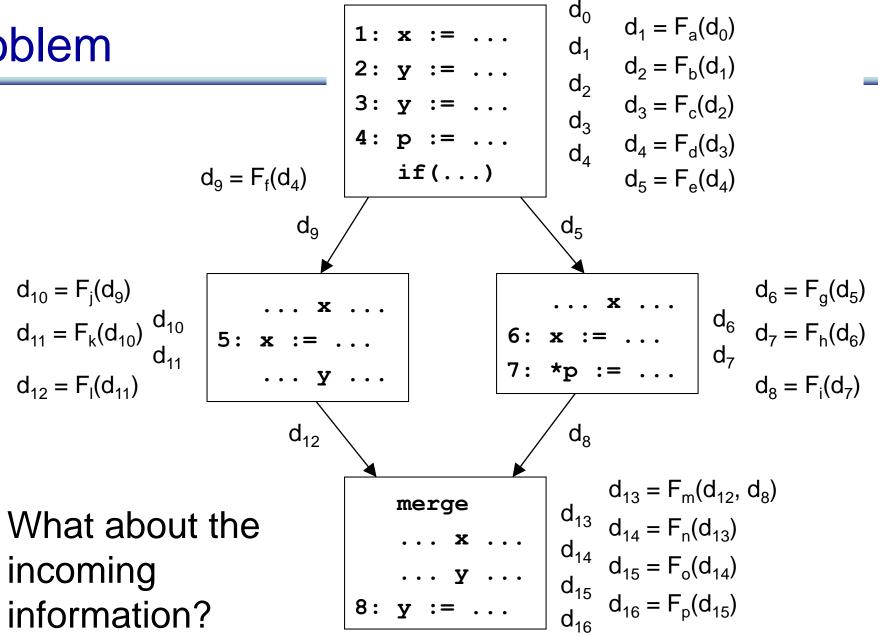
## Back to example



# How to find solutions for d<sub>i</sub>?

- This is a forward problem
  - given information flowing *in* to a node, can determine using the flow function the info flow *out* of the node
- To solve, simply propagate information forward through the control flow graph, using the flow functions
- What are the problems with this approach?

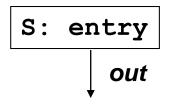
# First problem



# First problem

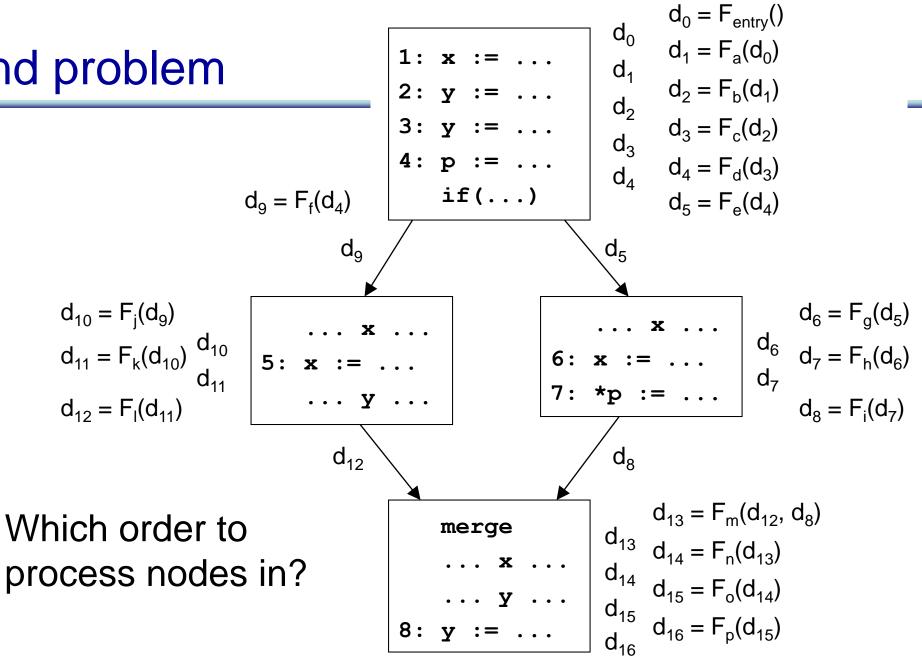
- What about the incoming information?
  - $d_0$  is not constrained
  - so where do we start?
- Need to constrain d<sub>0</sub>
- Two options:
  - explicitly state entry information
  - have an entry node whose flow function sets the information on entry (doesn't matter if entry node has an incoming edge, its flow function ignores any input)

## Entry node



#### out = { $X \rightarrow S \mid X \in Formals$ }

## Second problem



## Second problem

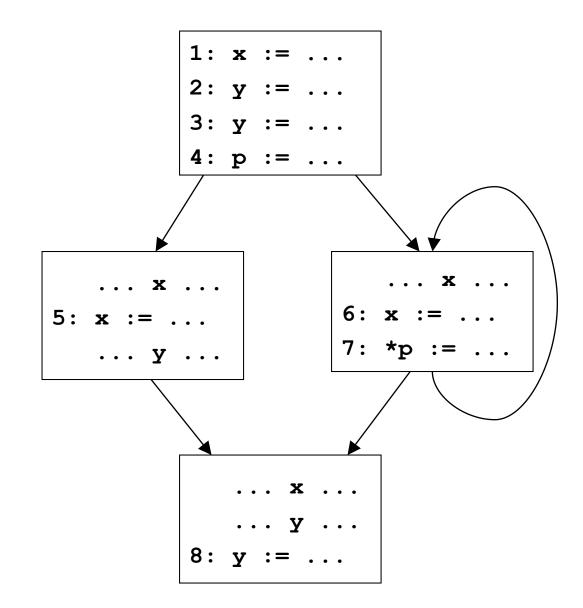
• Which order to process nodes in?

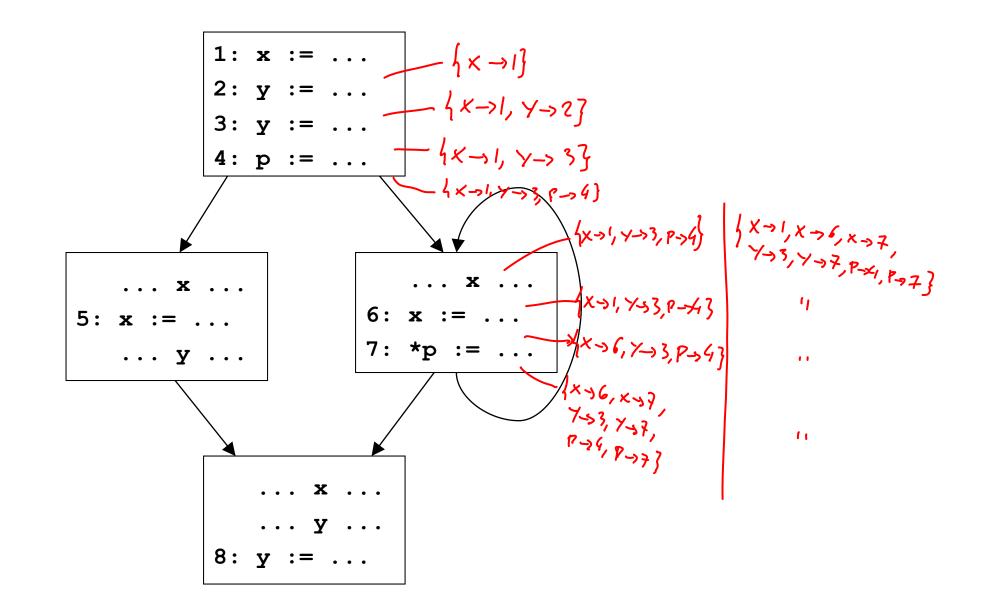
- Sort nodes in topological order
  - each node appears in the order after all of its predecessors
- Just run the flow functions for each of the nodes in the topological order

• What's the problem now?

## Second problem, prime

- When there are loops, there is no topological order!
- What to do?
- Let's try and see what we can do





# Worklist algorithm

- Initialize all d<sub>i</sub> to the empty set
- Store all nodes onto a worklist
- while worklist is not empty:
  - remove node n from worklist
  - apply flow function for node n
  - update the appropriate d<sub>i</sub>, and add nodes whose inputs have changed back onto worklist

```
let m: map from edge to computed value at edge
let worklist: work list of nodes
for each edge e in CFG do
  m(e) := \emptyset
for each node n do
   worklist.add(n)
while (worklist.empty.not) do
   let n := worklist.remove any;
   let info in := m(n.incoming edges);
   let info out := F(n, info in);
   for i := 0 .. info out.length-1 do
      if (m(n.outgoing edges[i]) ≠ info out[i])
         m(n.outgoing edges[i]) := info out[i];
         worklist.add(n.outgoing edges[i].dst);
```

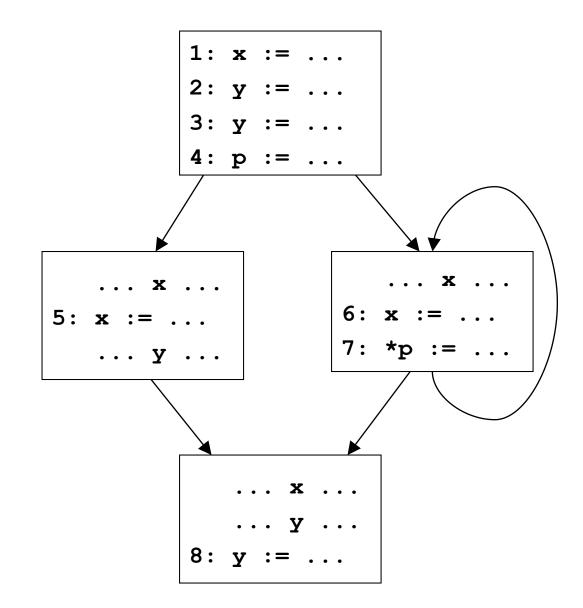
# Issues with worklist algorithm

## Two issues with worklist algorithm

- Ordering
  - In what order should the original nodes be added to the worklist?
  - What order should nodes be removed from the worklist?
- Does this algorithm terminate?

## Order of nodes

- Topological order assuming back-edges have been removed
- Reverse depth-first post-order
- Use an ordered worklist



## Termination

- Why is termination important?
- Can we stop the algorithm in the middle and just say we're done...
- No: we need to run it to completion, otherwise the results are not safe...

## Termination

 Assuming we're doing reaching defs, let's try to guarantee that the worklist loop terminates, regardless of what the flow function F does

```
while (worklist.empty.not) do
  let n := worklist.remove_any;
  let info_in := m(n.incoming_edges);
  let info_out := F(n, info_in);
  for i := 0 .. info_out.length-1 do
    if (m(n.outgoing_edges[i]) ≠ info_out[i])
      m(n.outgoing_edges[i]) := info_out[i];
      worklist.add(n.outgoing_edges[i].dst);
```

## Termination

 Assuming we're doing reaching defs, let's try to guarantee that the worklist loop terminates, regardless of what the flow function F does

## Structure of the domain

• We're using the structure of the domain outside of the flow functions

In general, it's useful to have a framework that formalizes this structure

• We will use lattices